



Factoring Perfect Cubes

$(a^3 - b^3) = (a - b)(a^2 + ab + b^2)$

$(a^3 + b^3) = (a + b)(a^2 - ab + b^2)$

SLIDE and DIVIDE

- 1) slide
- 2) factor
- 3) divide
- 4) bottoms up!!!



Factor completely:

$$\begin{aligned} 1) & x^6 - 16x^2 \\ & x^2(x^4 - 16) \\ & x^2(x^2 + 4)(x^2 - 4) \\ & x^2(x^2 + 4)(x + 2)(x - 2) \end{aligned}$$

SOAP

$$\begin{aligned} 2) & -7y^4 - 56y \\ & -7y(y^3 + 8) \\ & -7y(y + 2)(y^2 - 2y + 4) \end{aligned}$$

$$\begin{aligned} 3) & 3x^2 + 7x + 2 \\ & x^2 + 7x + 6 \\ & (x + \frac{6}{3})(x + \frac{1}{3}) \\ & (x + 2)(3x + 1) \end{aligned}$$

$$\begin{aligned} 4) & 3x^3 + 15x^2 - 12x - 60 \\ & 3[x^3 + 5x^2 - 4x - 20] \\ & 3[x^2(x + 5) - 4(x + 5)] \\ & 3(x^2 - 4)(x + 5) \\ & 3(x + 2)(x - 2)(x + 5) \end{aligned}$$

$$\begin{aligned} 5) & 8x^3 - 27 \\ & (2x - 3)(4x^2 + 6x + 9) \end{aligned}$$

$$\begin{aligned} 6) & 8x^2y - 20xy - 12y \\ & 4y(2x^2 - 5x - 3) \\ & 4y(2x + 1)(x - 3) \end{aligned}$$

$$\begin{aligned} 7) & 6x^2 + 11x - 10 \\ & (3x - 2)(2x + 5) \end{aligned}$$

$$\begin{aligned} 8) & -36x^3y + 15x^2y + 6xy \\ & -3xy(12x^2 - 5x - 2) \\ & -3xy(4x + 1)(3x - 2) \end{aligned}$$

$$\begin{aligned} 9) & -2x^3 + 2x \\ & -2x(x^2 - 1) \\ & -2x(x + 1)(x - 1) \end{aligned}$$

$$\begin{aligned} 10) & 60x^3 + 40x^2 - 135x - 90 \\ & 5(12x^3 + 8x^2 - 27x - 18) \\ & 5(4x^2(3x + 2) - 9(3x + 2)) \\ & 5(4x^2 - 9)(3x + 2) \\ & 5(2x + 3)(2x - 3)(3x + 2) \end{aligned}$$

$$\begin{aligned} 11) & x^4 - 29x^2 + 100 \\ & (x^2 - 25)(x^2 - 4) \\ & (x + 5)(x - 5)(x + 2)(x - 2) \end{aligned}$$

$$\begin{aligned} 12) & 54x^3 - 128 \\ & 2(27x^3 - 64) \\ & 2(3x - 4)(9x^2 + 12x + 16) \end{aligned}$$

Factor completely:

1. $5x - 15 = 5(x - 3)$

2. $yz^3 - 3yz^2 + 2yz = yz(z^2 - 3z + 2) = yz(z - 2)(z - 1)$

3. $z^2 - 49 = (z + 7)(z - 7)$

4. $64 - 25y^2 = (8 - 5y)(8 + 5y)$

5. $y^2 + 8y + 16 = (y + 4)^2$

6. $4z^2 - 4z + 1 = (2z - 1)^2$

7. $y^3 - 8 = (y - 2)(y^2 + 2y + 4)$

8. $27y^3 - 8 = (3y - 2)(9y^2 + 6y + 4)$

9. $1 - x^3 = (1 - x)(1 + x + x^2)$

10. $x^2 + 9x + 14 = (x + 7)(x + 2)$

11. $z^2 - 5z - 24 = (z - 8)(z + 3)$

12. $14u^2 - 33u - 5 = (7u + 1)(2u - 5)$

13. $12x^2 + 11x - 15 = (4x - 3)(3x + 5)$

14. $6x^2 + 11xy - 10y^2 = (3x - 2y)(2x + 5y)$

15. $x^3 - 4x^2 + 5x - 20 = x^2(x - 4) + 5(x - 4) = (x^2 + 5)(x - 4)$

16. $x^6 - 3x^4 + x^2 - 3 = x^4(x^2 - 3) + 1(x^2 - 3) = (x^4 + 1)(x^2 - 3)$

17. $2ac + 6ad - bc - 3bd = 2a(c + 3d) - b(c + 3d) = (2a - b)(c + 3d)$

18. $x^3 + x = x(x^2 + 1)$

19. $18y^3 + 48y^2 + 32y = 2y(9y^2 + 24y + 16) = 2y(3y + 4)^2$

20. $16y - y^3 = y(16 - y^2) = y(4 - y)(4 + y)$

21. $5y + 3y^2 - 2y^3 = -y(2y^2 - 3y - 5) = -y(2y - 5)(y + 1)$

22. $12x^2 + 22x - 20 = 2(6x^2 + 11x - 10) = 2(3x - 2)(2x + 5)$

23. $2ac - 2bd + 4ad - bc = 2ac + 4ad - bc - 2bd = 2a(c + 2d) - b(c + 2d) = (2a - b)(c + 2d)$

24. $x^3 - 3x^2 - 4x + 12 = x^2(x - 3) - 4(x - 3) = (x^2 - 4)(x - 3) = (x + 2)(x - 2)(x - 3)$